## Considerations for Implementing the Illinois Learning Standards for Mathematics

Intended Audience: Teachers, Administrators, Professional Development Coordinators



Learning Standards Leadership Team:

instruction and outcomes regarding the Illinois

**Description:** This rubric helps determine level of implementation for the Illinois Learning Standards based on 23 specific education. Concepts, including: Classroom, Assessment, Key Shifts, and Mathematical Practice Standards. This document can be used as a guide to navigate the full spectrum of implementation of the Illinois Learning Standards for Mathematics. This rubric is differentiated by grade band, including K-2, 3-5, 6-8, and High School documents.

#### Suggested Use for these Documents:

- Professional development coordinators could use this to lead a professional development workshop.
- Teachers, administrators or other stakeholders could use this to get an overview of the Implementation Considerations.
- Teachers could use this to determine what professional development they need or what classroom changes they still need.

#### **Materials Necessary:**

Considerations for Implementing the Illinois Learning Standards for Mathematics

#### Send questions and comments to:

plscomments@gmail.com

#### **Resource Links:**

K-2 Considerations for Implementation3-5 Considerations for Implementation6-8 Considerations for ImplementationHigh School Considerations for Implementation



Illinois State Board of Education www.isbe.net 100 N. 1st Street • Springfield, IL 62777 100 W. Randolph, Suite 14-300 • Chicago, IL 60601

#### **General Characteristics of the Illinois**

- Communicate expectations for Learning Standards for Mathematics.
- Professional development is aligned with the needs of the school/district with the implementation of the Illinois Learning Standards for Mathematics.
- Consider how professional development courses or workshops need to be differentiated in order to best suit the teachers. While some may be ready for advanced methods, others may need further assistance.
- District leaders should identify student learning priorities to target professional development that promotes the best practices to address student needs. The professional development plan must be systemic—long-range as well as short-range and fully articulated across the entire staff and grade spans.
- Meet regularly to discuss, update and plan for communications regarding upcoming PARCC assessments:

- Performance Level Descriptors
- Rubrics
- Item Task Prototypes
- Model Content Frameworks
- Evidence Statements
- Student Claims
- Meet regularly to plan how to communicate Illinois Learning Standards for Mathematics with stakeholders such as the community, school board and parents.
- Determine how they can facilitate and support collaboration among teachers that is focused on implementation of the standards.
- Dedicate staff to determine technology needs and how to integrate into the Illinois Learning Standards for Mathematics classroom.
- Develop a timeline to implement varied modes of assessments, including a range of pre, formative, summative and self-assessment measures.
- Analyze the current state of the school from a mathematics perspective with data from standardized test scores, state assessments, grades, and quantitative measures of student mathematics comprehension.

#### Materials

- Determine to what extent the existing instructional materials align with the standards and make a plan to address gaps, redundant content or unnecessary curriculum.
- Update instructional resources to align with the Illinois Learning Standards for Mathematics; evaluate resources for effectiveness.
- Examine the Publisher's Criteria before purchasing any new materials. <u>http://achievethecore.org/page/267/publishers-criteria-for-mathematics</u>

#### **Climate and Culture**

- Through frequent conversations, keep the focus on learning by acting as a catalyst to build partnerships with teacher leaders, instructional coaches, and technology specialists.
- Build collaborative cultures characterized by conversations centered around student learning and reflective inquiry, shared ownership, and short- and long-term thinking.
- Build trust through shared decision making, frequent communications, frequent visits to classrooms and consistency over time. In these cases, trust becomes a key driver toward a strong culture.
- Grow leaders by creating opportunities for teacher leadership to emerge and by sharing and distributing leadership throughout the school. This prepares schools for the reality that "many tasks... require many leaders."
- □ Build a Leadership Team for the Illinois Learning Standards for Mathematics implementation
- □ Examine ISBE's Comprehensive System of Learning Supports page for more information. <u>https://www.isbe.net/Pages/Learning-Supports.aspx</u>

#### Instructional Environment:

- □ Engage student interests in mathematics.
- Establish expectations that are easy to understand and meet.
- Provide all students with opportunities to engage with mathematics of appropriate complexity for the grade level.
- Engage students in a productive struggle through discussion and other supports that build towards independence.
- Include appropriate supports for students who are ELL, have disabilities, or read or write well below grade level.
- □ Include extensions and/or more advanced math tasks for students who are well above grade level.
- □ Integrate available technology and media throughout curriculum and instruction.

A research base is connected to this instrument that does include Charlotte Danielson's Framework for evaluation, however, this tool is not meant to serve as an evaluation tool. This tool is only meant to serve as a connection in thinking for the teacher or administrator to formulate a synthesis from the shifts of the Illinois Learnings Standards to practice in the classroom. Therefore, in no way should it be implied that a beginning implementation level serve as an unsatisfactory or basic level of teacher performance.

### Charlotte Danielson's FRAMEWORK FOR TEACHING

DOMAIN 1: Planning and Preparation	DOMAIN 2: The Classroom Environment
<ul> <li>Demonstrating Knowledge of Content and Pedagogy</li> <li>Content knowledge</li> <li>Prerequisite relationships</li> <li>Content pedagogy</li> </ul>	<ul> <li>2a Creating an Environment of Respect and Rapport</li> <li>Teacher interaction with students</li> <li>Student interaction with students</li> </ul>
<ul> <li>1b Demonstrating Knowledge of Students</li> <li>Child development • Learning process • Special needs</li> <li>Student skills, knowledge, and proficiency</li> <li>Interests and cultural heritage</li> </ul>	<ul> <li>2b Establishing a Culture for Learning</li> <li>Importance of content</li> <li>Expectations for learning and behavior</li> <li>Student pride in work</li> </ul>
<ul> <li>1c Setting Instructional Outcomes</li> <li>Value, sequence, and alignment</li> <li>Clarity</li> <li>Balance</li> <li>Suitability for diverse learners</li> </ul>	<ul> <li>2c Managing Classroom Procedures         <ul> <li>Instructional groups</li> <li>Transitions</li> <li>Materials and supplies</li> <li>Non-instructional duties</li> <li>Supervision of volunteers and paraprofessionals</li> </ul> </li> </ul>
<ul> <li>1d Demonstrating Knowledge of Resources         <ul> <li>For classroom</li> <li>To extend content knowledge</li> <li>For students</li> </ul> </li> <li>1e Designing Coherent Instruction         <ul> <li>Learning activities</li> <li>Instructional materials and resources</li> </ul> </li> </ul>	<ul> <li>2d Managing Student Behavior</li> <li>• Expectations</li> <li>• Monitoring behavior</li> <li>• Response to misbehavior</li> </ul>
<ul> <li>Instructional groups</li> <li>Lesson and unit structure</li> <li>1f Designing Student Assessments</li> <li>Congruence with outcomes</li> <li>Criteria and standards</li> <li>Formative assessments</li> <li>Use for planning</li> </ul>	<ul> <li>2e Organizing Physical Space</li> <li>• Safety and accessibility</li> <li>• Arrangement of furniture and resources</li> </ul>
DOMAIN 4: Professional Responsibilities	DOMAIN 3: Instruction
DOMAIN 4: Professional Responsibilities 4a Reflecting on Teaching • Accuracy • Use in future teaching	3a Communicating With Students
<ul> <li>4a Reflecting on Teaching <ul> <li>Accuracy</li> <li>Use in future teaching</li> </ul> </li> <li>4b Maintaining Accurate Records <ul> <li>Student completion of assignments</li> </ul> </li> </ul>	<ul> <li>3a Communicating With Students</li> <li>• Expectations for learning • Directions and procedures</li> <li>• Explanations of content • Use of oral and written language</li> </ul>
<ul> <li>4a Reflecting on Teaching <ul> <li>Accuracy</li> <li>Use in future teaching</li> </ul> </li> <li>4b Maintaining Accurate Records <ul> <li>Student completion of assignments</li> <li>Student progress in learning</li> <li>Non-instructional records</li> </ul> </li> <li>4c Communicating with Families <ul> <li>About instructional program</li> <li>About individual students</li> </ul> </li> </ul>	<ul> <li>3a Communicating With Students <ul> <li>Expectations for learning</li> <li>Directions and procedures</li> <li>Explanations of content</li> <li>Use of oral and written language</li> </ul> </li> <li>3b Using Questioning and Discussion Techniques <ul> <li>Quality of questions</li> <li>Discussion techniques</li> <li>Student participation</li> </ul> </li> <li>3c Engaging Students in Learning</li> </ul>
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<ul> <li>4a Reflecting on Teaching <ul> <li>Accuracy</li> <li>Use in future teaching</li> </ul> </li> <li>4b Maintaining Accurate Records <ul> <li>Student completion of assignments</li> <li>Student progress in learning</li> <li>Non-instructional records</li> </ul> </li> <li>4c Communicating with Families <ul> <li>About instructional program</li> <li>About instructional program</li> </ul> </li> <li>4d Participating in a Professional Community <ul> <li>Relationships with colleagues</li> <li>Participation in school projects</li> </ul> </li> </ul>	<ul> <li>3a Communicating With Students <ul> <li>Expectations for learning</li> <li>Directions and procedures</li> <li>Explanations of content</li> <li>Use of oral and written language</li> </ul> </li> <li>3b Using Questioning and Discussion Techniques <ul> <li>Quality of questions</li> <li>Discussion techniques</li> <li>Student participation</li> </ul> </li> <li>3c Engaging Students in Learning <ul> <li>Activities and assignments</li> <li>Student groups</li> <li>Instructional materials and resources</li> <li>Structure and pacing</li> </ul> </li> </ul>

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### Mathematics Grades 3-5:

Mathematics Grades 3-5: General Considerations for an Illinois Learning Standards Classroom

Category & Example of Danielson Connection	Full Implementation	Partial Implementation	Beginning Implementation
Primary Resources	The teacher has read , references when appropriate & bases their instruction on the <u>Illinois Learning Standards for</u> <u>Mathematics, Progression Documents, The Publishers'</u> <u>Criteria, EQuIP Rubric, PARCC Model Content Frameworks,</u> and the <u>PARCC Evidence Statements and Informational</u> Guides.	The teacher has read and sometimes bases their instruction on the <u>Illinois Learning</u> <u>Standards for Mathematics</u> , appropriate <u>Progression Documents</u> , and the <u>PARCC</u> <u>Model Content Frameworks</u> .	The teacher has read and occasionally bases their instruction on the <u>Illinois Learning</u> <u>Standards for Mathematics</u> .
Materials (Curriculum)	<ul> <li>The teacher has researched alignment of all coursework material to the appropriate grade-level of the Illinois Learning Standards.</li> <li>The teacher has utilized the <u>Toolkit for Evaluating the</u> <u>Alignment of Instructional and Assessment Materials to</u> <u>the CCSS</u> to identify common pitfalls and necessary steps in creating a curriculum that is truly aligned to the letter and spirit of the Illinois Learning Standards.</li> </ul>	The teacher occasionally utilizes the <u>Toolkit</u> for Evaluating the Alignment of Instructional and Assessment Materials to the CCSS to identify common pitfalls and necessary steps in creating a curriculum that is truly aligned to the letter and spirit of the Illinois Learning Standards.	The teacher has not read or does not use <u>the</u> <u>Toolkit for Evaluating the Alignment of</u> <u>Instructional and Assessment Materials to the</u> <u>CCSS</u> .
Classroom Culture	<ul> <li>The teacher provides a safe and welcoming classroom environment that promotes interaction, communication, collaboration, and intellectual risk taking.</li> <li>The teacher directs the communication and discovery of mathematical ideas by posing good questions, engaging students in worthwhile tasks, creating a culture that fosters students' creativity and understanding of mathematics.</li> <li>The teacher frequently uses a student-centered approach, where the teacher's role is facilitator.</li> </ul>	<ul> <li>The teacher provides a safe and welcoming classroom environment that often promotes interaction, communication, and collaboration.</li> <li>The teacher often provides direct instruction and expects students to answer similar problems with the same process. Students rarely feel comfortable taking intellectual risks.</li> <li>The teacher provides students with worthwhile tasks and classroom time to work in pairs or small groups to find the solutions.</li> <li>The teacher sometimes uses a student- centered approach, where the teacher's role is facilitator.</li> </ul>	<ul> <li>The teacher provides a safe classroom environment where students are expected to remain silent unless called upon, take good and accurate notes, follow all directions, and work independently.</li> <li>The teacher often provides direct instruction to students and expects students to answer similar problems with the same process that was demonstrated.</li> <li>The teacher rarely provides time for students to collaborate or communicate with one another.</li> <li>The teacher rarely uses a student- centered approach, where the teacher's role is facilitator.</li> </ul>
Assessment Literacy	<ul> <li>The teacher consistently uses assessment concepts and terminology correctly. [As defined in the Guidelines for Classroom Assessment]</li> </ul>	The teacher does not consistently use     assessment concepts and terminology     correctly.	The teacher does not use assessment concepts or terminology correctly.

Category	Full Implementation	Partial Implementation	Beginning Implementation
Linking instruction and assessment	<ul> <li>The teacher implements both standards-aligned instruction and ongoing assessment aligned to standards to promote learning.</li> </ul>	<ul> <li>The teacher inconsistently implements both standards-aligned instruction and ongoing assessment aligned to standards to promote learning.</li> </ul>	<ul> <li>The teacher does not implement both standards-aligned instruction and ongoing assessment aligned to standards to promote learning.</li> </ul>
Selecting and designing assessment	<ul> <li>The teacher consistently selects and designs assessments based on the purpose for the assessment including what decisions will be influences by the results and the best method for assessing the expectations.</li> </ul>	<ul> <li>The teacher inconsistently selects and designs assessments based on the purpose for the assessment including what decisions will be influences by the results and the best method for assessing the expectations.</li> </ul>	<ul> <li>The teacher infrequently selects and designs assessments based on the purpose for the assessment including what decisions will be influences by the results and the best method for assessing the expectations.</li> </ul>
Administer and score assessment	• The teacher conscientiously administers and scores the Illinois Learning Standards aligned assessments for the intended purpose, with accommodations as appropriate.	• The teacher inconsistently administers and scores assessments correctly.	The teacher seldom administers and scores assessments correctly.
Feedback	<ul> <li>The teacher consistently provides constructive feedback based assessment data to students to support attainment of the Illinois Learning Standards expectations.</li> </ul>	<ul> <li>The teacher inconsistently provides constructive feedback based assessment data to students to support attainment of the Illinois Learning Standards expectations.</li> </ul>	• The teacher seldom provides constructive feedback based assessment data to students to support attainment of the Illinois Learning Standards expectations.
Analyzing and using data	• The teacher consistently administers assessments (formative, interim and summative) and accurately analyzes assessment data to inform instruction.	• The teacher inconsistently administers assessments (formative, interim and summative) and analyzes assessment data to inform instruction.	• The teacher infrequently administers assessments (formative, interim and summative) and does not analyze assessment data to inform instruction.
Using data to identify trends	<ul> <li>The teacher independently and collaboratively works with team/grade level members to analyze data, identify trends in achievement, and suggest adjustments to curriculum to meet the Illinois Learning Standards expectations.</li> </ul>		

Category	Full Implementation	Partial Implementation	Beginning Implementation
Reporting	• The teacher reports assessment data reflecting progress or attainment of the Illinois Learning Standards expectations clearly and concisely to appropriate stakeholders in a timely manner.	<ul> <li>The teacher inconsistently reports assessment data reflecting progress or attainment of the Illinois Learning Standards expectations clearly and concisely to appropriate stakeholders.</li> </ul>	<ul> <li>The teacher seldom reports assessment data reflecting progress or attainment of the Illinois Learning Standards expectations clearly and concisely to appropriate stakeholders in a timely manner.</li> </ul>
Vertical Alignment	<ul> <li>The teacher has read the grade-level <u>Illinois Learning</u> <u>Standards for Mathematics</u> for the grade above and below the class they are teaching.</li> <li>The teacher has met with other teachers in the same grade-level to discuss changes that have occurred, including new material to the grade-level and the material that is no longer in this grade.</li> <li>The teacher team has met with representatives from the grade above and the grade below to discuss any necessary transition steps as students interact with changing curriculum.</li> <li>The teacher recognizes what knowledge the students bring with them when entering the classroom and connects new information to what they will learn the following year.</li> <li>The teacher always makes connections.</li> </ul>	<ul> <li>The teacher has read the grade-level <u>Illinois Learning Standards for</u> <u>Mathematics</u> for the grade above and below the class they are teaching.</li> <li>The teacher has noted changes to the curriculum, including new material to the grade-level and material that is no longer in this grade.</li> <li>The teacher recognizes what knowledge the students bring with them when entering the classroom and connects new information to what they will learn the following year.</li> <li>The teacher sometimes makes connections.</li> </ul>	<ul> <li>The teacher has read the grade-level <u>Illinois Learning Standards for</u> <u>Mathematics</u> for the grade above and below the class they are teaching.</li> <li>The teacher rarely makes connections.</li> </ul>



# **Mathematics: Key Shifts**

Category	Full Implementation	Partial Implementation	Beginning Implementation
Focus	<ul> <li>The teacher spends a significant amount of classroom time discussing grade-level, content-aligned standards that have been designated Major work by the PARCC Model Content Frameworks. In grades 3-5 students focus on developing an understanding and the fluency (Fluency is defined as efficient and accurate methods for solving problems. Students use flexibility in choosing methods and can explain their chosen method.) of multiplication, division, fractions, and decimals (place-value). Significant time is also spent on describing and analyzing two-dimensional shapes, properties of figures, and finding the volume of three-dimensional figures.</li> <li>The teacher revisits the critical areas (listed at the beginning of the grade-level standards in the New Illinois Learning Standards) throughout the year.</li> <li>The teacher allows students time to explore these key ideas and develop a strong conceptual understanding and procedural skill in a connected and meaningful way related to the world around them.</li> <li>Teachers do not add curriculum that is not directly stated in the appropriate grade-level standards.</li> </ul>	<ul> <li>The teacher creates and/or selects lessons that make some natural connections between grade-level work, or between standards, domains, and clusters.</li> <li>The teacher occasionally develops lessons or units that follow the Progression documents, the PARCC Model Content Frameworks and the PARCC Evidence Statements and Informational Guides.</li> <li>The teacher occasionally points out the connections to the students.</li> </ul>	<ul> <li>The teacher has not read and/or is not developing units and lessons based on the Major work as defined by the <u>PARCC</u><u>Model Content Frameworks</u>.</li> <li>The teacher occasionally revisits the critical areas (listed at the beginning of the grade-level standards in the New Illinois Learning Standards) throughout the year.</li> <li>The teacher occasionally adds curriculum that is not stated in the appropriate grade-level standards.</li> </ul>

Category	Full Implementation	Partial Implementation	Beginning Implementation
Coherence	<ul> <li>The teacher creates and/or selects lessons that make natural connections to previous grade-level work, lay a natural foundation for subsequent grade-level work and make apparent connections between standards, domains and clusters.</li> <li>Material is developed referencing the <u>Progression</u> <u>Documents</u>, the <u>PARCC Model Content Frameworks</u>, and the <u>PARCC Evidence Statements and Informational Guides</u>.</li> <li>Students should see partitioning of shapes as a visual representation of multiplication and division, scaled picture graphs can apply multiplication, ability to change decimals to fractions with denominators as multiples of ten, ability to use all four operations for measurement of liquid volume, mass and time, use of line plots with fractions, and connection of decimals to metric system and powers of ten.</li> <li>Mathematics builds upon itself creating an inherent evolution that makes sense.</li> </ul>	<ul> <li>The teacher occasionally provides tasks for students to develop their understanding of mathematical concepts, become fluent with appropriate procedural skill, and recognize how and when mathematical concepts apply to the world around them.</li> <li>The teacher occasional coherently combines these into a lesson. Occasionally a teacher only addresses one of the three ideas in situations where more than one should be addressed: understanding, skill, or application.</li> </ul>	<ul> <li>The teacher creates and/or selects lessons that make little connection to previous grade-level work, subsequent grade-level work, or connections between standards, domains, and clusters.</li> <li>The teacher has not read or does not reference the <u>Progression Documents</u>, the <u>PARCC Model Content Frameworks</u> or the <u>PARCC Evidence Statements and Informational Guides</u>. Mathematical information is presented in a disjointed fashion.</li> </ul>
Rigor	<ul> <li>The teacher coherently combines understanding, skill, and application into all tasks and lessons whenever possible.</li> <li>The teacher provides sufficient opportunities for students to develop their understanding of fractions and decimals as numbers, including number line representation. Tasks promote fluency in multiplication and division, addition, subtraction, and multiplication of multi-digit numbers. Tasks provide mathematical insight into the world around including application of four operations to liquid volume, mass, time, and line plots (including fractions).</li> <li>The teacher creates lessons and assessments representing the difficulty level inherent in the <u>PARCC released items</u>, the <u>Progression Documents</u>, and <u>Illustrative Mathematics</u> tasks.</li> </ul>	<ul> <li>The teacher occasionally provides tasks for students to develop their understanding of mathematical concepts, become fluent with appropriate procedural skill, and recognize how and when mathematical concepts apply to the world around them.</li> <li>The teacher occasional coherently combines these into a lesson. Occasionally a teacher only addresses one of the three ideas in situations where more than one should be addressed: understanding, skill, or application.</li> </ul>	<ul> <li>The teacher treats most mathematics and tasks as separate ideas in which a student only concentrates on learning conceptual understanding, procedural skill, or application.</li> <li>The teacher does not often coherently combine understanding, skill, and application into a task, lesson, or assessment.</li> </ul>



## **The Standards for Mathematical Practice**

**The Definition of a Worthwhile Task:** A worthwhile task cohesively aligns to both common core grade-level content standards and standards for mathematical practice. A task builds upon students' previous knowledge and provides opportunity for students to develop conceptual understanding and obtain procedural skill and fluency. Tasks include a wide variety of mediums and student products. Tasks vary in modalities, learning styles, and length of time required to develop solutions. Tasks require students to communicate their mathematical reasoning.

Category	Full Implementation	Partial Implementation	Beginning Implementation
MP1 - Make sense of problems and persevere in solving them	<ul> <li>A 3rd-5th grade teacher supports Mathematical Practice Standard 1 by providing worthwhile tasks that require students to work past the point that they would normally want to give up.</li> <li>The teacher provides time and tasks that require students to explain to themselves the meaning of a problem, look for ways to solve it, make attempts, and recognize when their attempt is not working and change course to try again. Students work independently or collaboratively to seek the meaning of a problem and look for efficient ways to represent and solve it.</li> <li>The teacher encourages students to use another method to check their work.</li> <li>The teacher allows the student's time to consider their own process and results without providing constant scaffolding, verifying answers, or limiting methods. Students may show signs of struggle, but have enough tools to rely on to work through this. <u>Example Task</u></li> </ul>	<ul> <li>The teacher provides many worthwhile tasks that require students to work past the point they would normally want to give up.</li> <li>The teacher discusses and models the process to making sense of mathematical problems.</li> <li>The teacher occasionally reminds students or prompts students of the process.</li> <li>The teacher occasionally limits discussion or time on problems by providing direct instruction, scaffolding, answers, or demonstrating personal approach.</li> </ul>	<ul> <li>The teacher rarely provides worthwhile tasks or appropriate wait time. Often the teacher provides direct instruction on how to solve the problem.</li> <li>The teacher does not encourage students to check their answers to see if they make sense.</li> <li>Most tasks are completed the same way by everyone in the classroom with little to no discussion on the variety of strategies that could be used.</li> </ul>

Category	Full Implementation	Partial Implementation	Beginning Implementation
MP2 - Reason abstractly and quantitatively	<ul> <li>A 3rd-5th grade teacher supports Mathematical Practice Standard 2 by engaging students in grade-level worthwhile tasks that challenge students to recognize that a number represents a specific quantity, numbers connect to written symbols, and numbers connect to create logical representations of a problem.</li> <li>The tasks provide opportunities for students to decontextualize the information from a word problem, but then treat the numbers as if they are separate from the word problem- sometimes changing order where mathematically appropriate, but not appropriate within the scenario.</li> <li>Once a mathematical answer is found, the students contextualize, by putting the answer back into the scenario and checking to see if it makes sense.</li> <li>In fourth grade, students need to be able to compute and interpret remainders in real-world division problems.</li> <li>Tasks challenge students across a wide range of learning styles and modalities. Example Task</li> </ul>	<ul> <li>Often the teacher supports Mathematical Practice Standard 2 by engaging students in grade-level worthwhile tasks that challenge students to make sense of quantities and their relationships in problem situations.</li> <li>Students recognize that a number represents a specific quantity but work on their connections to symbols and logical representations (expressions) of a problem.</li> <li>Some of the tasks challenge students across a wide range of learning styles and modalities while encouraging the use of quantitative reasoning.</li> </ul>	<ul> <li>Occasionally the teacher provides tasks in which students must use their knowledge of numbers representing a specific quantity to connect the quantity to written symbols and create a logical representation (expression) of the problem.</li> <li>Little to no time is spent in understanding the relationships of the quantities, units involved, or properties of operations and objects.</li> <li>Many of the tasks do not challenge students because they do not vary in their language, expectations, or abstract and quantitative reasoning skills.</li> </ul>
MP3 - Construct viable arguments and critique the reasoning of others	<ul> <li>A 3rd-5th grade teacher supports Mathematical Practice Standard 3 by engaging students in worthwhile tasks that elicit and challenge students' mathematical communication skills. Tasks provide opportunities for students to use assumptions, definitions, concrete objects, and previously established results in constructing arguments.</li> <li>The teacher provides significant class time for students to refine their mathematical communication skills as they participate in mathematical discussions, and ask students "How did you get that?" and "Why is that true?" and honors the multiple strategies students use to solve problems/tasks.</li> <li>The teacher provides ample collaborative time and varied tasks that promote both written and oral communication.</li> <li>The teacher provides re-engagement tasks, where students re-engage the task and critique the work of others.</li> <li>Example Task</li> </ul>	<ul> <li>The teacher provides many worthwhile tasks that elicit and challenge students' mathematical communication skills.</li> <li>The teacher often provides opportunities for students to use assumptions, definitions, concrete objects, and previously established results in constructing arguments.</li> <li>The teacher often provides collaborative time in the classroom for students to practice supporting their mathematics with both written and oral communication.</li> </ul>	<ul> <li>Occasionally the teacher provides tasks that elicit and challenge students' mathematical communication skills.</li> <li>The teacher occasionally provides opportunities for students to work in pairs or small groups to develop their ability to construct a mathematical argument or to express their reasoning to others.</li> </ul>

Category	Full Implementation	Partial Implementation	Beginning Implementation
MP4 - Model with mathematics	<ul> <li>A 3rd-5th grade teacher supports Mathematical Practice Standard 4 by providing worthwhile tasks that incorporate a wide variety of mediums and tools to understand and solve problems arising in everyday life, society, and the workplace.</li> <li>The teacher promotes the relationship between mathematics and the world around them in meaningful and appropriate ways, encouraging students to view mathematics and everyday life as connected.</li> <li>The teacher encourages students to make connections from the math they are working on to their real-life circumstances.</li> <li>The teacher provides tasks that demonstrate this connection and allows students to solve the problems using any model the feel is most appropriate including numbers, equations, mathematical language (words), pictures, concrete objects, charts, lists, graphs, etc.</li> <li>The teacher develops a natural practice of reflection, to see if results and models make sense. Students begin evaluating the efficiency of the model they used to solve the problem. <u>Sample Task</u></li> </ul>	<ul> <li>The teacher often provides worthwhile tasks that incorporate a variety of mediums and tools to understand and solve problems arising in everyday life.</li> <li>The teacher encourages students to use any model they feel is most appropriate and to consider the efficiency of that model.</li> <li>The teacher makes clear connections between the math students are working on to students' real-life circumstances.</li> <li>The teacher reminds students to reflect and check their work.</li> </ul>	<ul> <li>The teacher provides few worthwhile tasks involving the modeling of mathematics and the connections that exist between mathematical concepts and everyday life.</li> <li>The teacher demonstrates several ways to model with mathematics but limits the resources available or acceptable solutions in an effort to maintain uniformity.</li> <li>The teacher often reminds students to reflect and check their work.</li> <li>The teacher spends little time helping students consider the efficiency of models or instills in students a need to do so.</li> </ul>
MP6 - Attend to precision	<ul> <li>A 3rd-5th grade teacher supports Mathematical Practice Standard 6 by communicating precisely using proper mathematical terms and definitions, including equation, equals, rhombus, ellipse, commutative, associative and distributive properties.</li> <li>The teacher provides worthwhile tasks that develop students' knowledge and understanding of mathematical language, units, symbols and definitions, and encourages students to use clear and precise language in their own discussions.</li> <li>The teacher provides a variety of tasks that address the necessity for attention to detail with units (recording area, labeling line plots, volume, etc.), proper use of symbols, ability to calculate accurately and efficiently, and grade-level appropriate mathematical terminology. <u>Sample Task</u></li> </ul>	<ul> <li>The teacher often provides worthwhile tasks that develop students' knowledge and understanding of mathematical language and definitions.</li> <li>The teacher occasionally uses non-precise language and sometimes teaches material using mnemonics and/or "tricks".</li> <li>The teacher occasionally encourages students to use precise language, units, and symbols.</li> <li>The teacher often discusses the importance of calculating accurately and efficiently.</li> </ul>	<ul> <li>The teacher does not consistently communicate mathematics with precise or proper mathematical terminology.</li> <li>The teacher utilizes mnemonics and/or "tricks" when teaching new mathematical processes.</li> <li>The teacher rarely stresses the importance of using proper units and symbols.</li> <li>The teacher rarely provides worthwhile tasks that develop students' understanding of mathematical language and definitions.</li> </ul>

Category	Full Implementation	Partial Implementation	Beginning Implementation
MP7 - Look for and make use of structure	<ul> <li>A 3rd-5th grade teacher supports practice standard 7 by providing worthwhile tasks that develop students' ability to recognize patterns or structures in mathematics and then use those to efficiently solve a problem.</li> <li>The teacher encourages students to communicate patterns or structures they see and how they use that knowledge in problem-solving (properties of operations-multiplication and division, partial products models, and add, subtract, multiply and divide whole numbers, fractions, and decimals).</li> <li>The teacher provides tasks that begin building up students' ability to recognize opportunities to see complicated things as a single object or as being composed of several objects.</li> <li>The teacher encourages students to look closely at all problems and discern a structure. Sample Task</li> </ul>	<ul> <li>The teacher often provides worthwhile tasks that develop students' ability to recognize patterns or structures in mathematics.</li> <li>The teacher often points out any patterns or structures in a task to the students and explains how this information can be useful when solving the problem.</li> <li>The teacher occasionally encourages students to find the pattern or structure on their own.</li> </ul>	<ul> <li>The teacher occasionally provides worthwhile tasks that develop students' ability to recognize patterns or structures in mathematics.</li> <li>The teacher points out these patterns and structures and explains how the information can be useful when solving the problem.</li> <li>The teacher provides little to no time for students to communicate the patterns or structures that they see and how they would use them in problem-solving.</li> </ul>
MP8 - Look for and express regularity in repeated reasoning	<ul> <li>A 3rd-5th grade teacher supports Mathematical Practice Standard 8 by engaging students in worthwhile tasks that provide opportunity for students to develop general methods and shortcuts by recognizing patterns.</li> <li>In third grade, students may use the distributive property as a strategy for using products they know to solve products they do not know.</li> <li>In fourth grade, students may use models to explain algorithms, like using a visual fraction model to write equivalent fractions.</li> <li>In fifth grade, students see the pattern that exists when multiplying or dividing a number by a power of ten. <u>Sample Task</u></li> </ul>	<ul> <li>The teacher often provides worthwhile tasks that provide opportunity to develop general methods and shortcuts by recognizing patterns.</li> <li>The teacher often points these short cuts out to the students.</li> <li>The teacher occasionally provides tasks and time for students to develop general methods or shortcuts without direct instruction.</li> </ul>	<ul> <li>The teacher occasionally provides worthwhile tasks that develop general methods and shortcuts.</li> <li>The teacher often provides the students with the insight into the patterns and connects them to a general method or shortcut for the students.</li> </ul>